



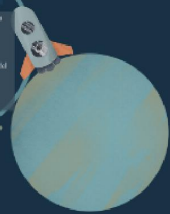
Making Cents of Space Travel: The Economics of In-Space Propulsion

Manju Bangalore



Overall Project

- Create equations for delta-v and top line as functions of mass, mass, specific impulse and efficiency
- Develop cost based space alt model including mass and costs for all subsystems



Scalable Analysis

- Range
- Mass
- Specific Impulse
- Efficiency
- Cost
- Subsystem
- Launch cost (per specific volume)

Cost to LEO equation

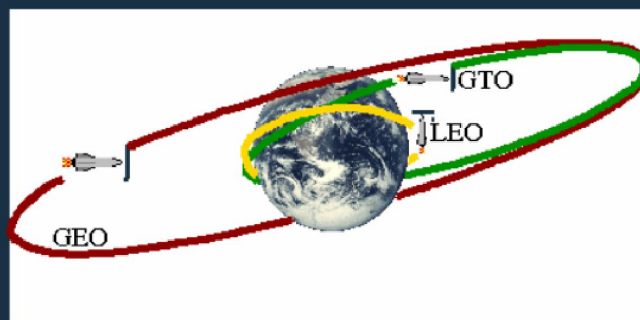
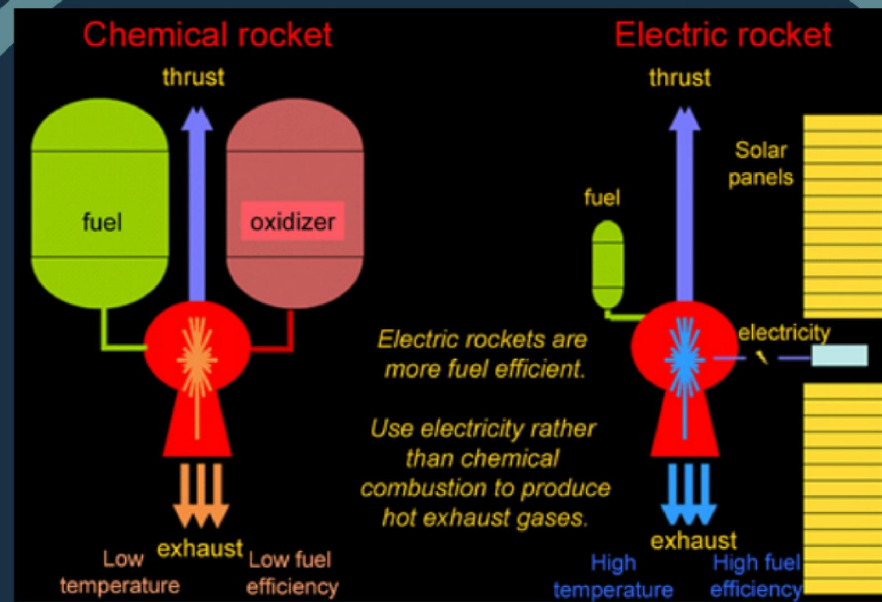
Mass	
Specific Impulse	
Efficiency	
Launch cost	

Minimum Mass Weight

Minimum Mass Weight
Minimum Mass Weight
Minimum Mass Weight

Making Cents of Space Travel: The Economics of In-Space Propulsion

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Overall Project

- Create equations for Δv and trip time as functions of power, mass, specific impulse, and efficiency
- Develop excel-based spacecraft model including mass and costs for all subsystems

Procurement of Equations

- Utilized SEPPSPOT, MATLAB, and Excel
- Cases vary by orbit, specific impulse, efficiency, shadowing, and power

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	
1	casenu	MO	PO	isp	Eff	u	fo	Time	SMA	Ecc	Incl	Mass	RPow	Pow	Flunc	Per	dv	acc
2	1	4000	0.5	800	30	9.53E-07	28.72	42158	0.00021	0.001	2858.4	1	0.48	0.1	23.929	2.6362	9.55657E-09	
3	17	4000	0.75	800	30	8.26E-11	19.16	42164	0	0	2858	1	0.73	0.1	23.934	2.6372	1.43349E-08	
4	5	4000	0.5	900	30	5.68E-14	32.9	42164	0	0	2966.5	1	0.48	0.1	23.934	2.6381	8.49473E-09	
5	21	4000	0.75	900	30	8.35E-10	21.93	42164	0	0	2966.8	1	0.73	0.1	23.934	2.6373	1.27421E-08	
6	37	4000	1	900	30	2.07E-07	16.45	42161	4.00E-05	0	2966.8	1	0.97	0.1	23.932	2.6373	1.69895E-08	
7	53	4000	1.25	900	30	3.74E-12	13.16	42164	0	0	2966.7	1	1.21	0.1	23.934	2.6377	2.12368E-08	
8	85	4000	1.75	900	30	2.92E-09	9.4	42164	3.00E-05	0.001	2966.7	1	1.69	0.1	23.934	2.6376	2.97316E-08	
9	9	4000	0.5	1000	30	2.72E-11	37.04	42164	0	0	3057.1	1	0.49	0.1	23.934	2.6363	7.64526E-09	
10	25	4000	0.75	1000	30	1.75E-08	24.71	42164	3.00E-05	0.001	3056.9	1	0.73	0.1	23.934	2.6369	1.14679E-08	
11	41	4000	1	1000	30	2.63E-12	18.53	42164	0	0	3056.8	1	0.97	0.1	23.934	2.6374	1.52905E-08	
12	57	4000	1.25	1000	30	3.41E-11	14.83	42164	0	0	3056.7	1	1.21	0.1	23.934	2.6375	1.91131E-08	
13	73	4000	1.5	1000	30	4.60E-11	12.36	42164	0	0	3056.7	1	1.45	0.1	23.934	2.6375	2.29358E-08	
14	89	4000	1.75	1000	30	7.87E-09	10.59	42165	1.00E-05	0	3056.7	1	1.69	0.1	23.935	2.6375	2.67584E-08	
15	29	4000	0.75	1100	30	1.35E-10	27.49	42164	0	0	3132.6	1	0.73	0.1	23.934	2.6367	1.04254E-08	
16	61	4000	1.25	1100	30	8.08E-10	16.5	42164	0	0	3132.4	1	1.21	0.1	23.935	2.6374	1.73756E-08	
17	93	4000	1.75	1100	30	4.18E-12	11.79	42164	0	0	3132.2	1	1.69	0.1	23.934	2.638	2.43258E-08	
18	1	4000	0.5	1200	30	3.75E-12	45.38	42164	0	0	3197.5	1	0.49	0.1	23.934	2.6351	6.37105E-09	
19	129	4000	1.5	1200	30	6.99E-08	15.14	42163	0.00018	0.01	3197	1	1.45	0.1	23.934	2.6371	1.91131E-08	
20	161	4000	1.75	1200	30	7.54E-10	12.98	42164	1.00E-05	0	3196.8	1	1.69	0.1	23.934	2.6377	2.22987E-08	
21	33	4000	0.75	1200	30	3.44E-10	30.28	42164	2.00E-05	0	3197.1	1	0.73	0.1	23.934	2.6366	9.55657E-09	
22	65	4000	1	1200	30	4.46E-14	22.72	42164	0	0	3197	1	0.97	0.1	23.934	2.637	1.27421E-08	
23	9	4000	0.5	1400	30	9.03E-07	53.7	42169	0.00028	0.019	3301.3	1	0.49	0.1	23.939	2.6358	5.4609E-09	
24	105	4000	1.25	1400	30	1.42E-08	21.53	42163	5.00E-05	0.001	3301	1	1.21	0.1	23.934	2.6371	1.36522E-08	
25	137	4000	1.5	1400	30	3.59E-10	17.94	42164	0	0	3300.9	1	1.45	0.1	23.934	2.6373	1.63827E-08	
26	169	4000	1.75	1400	30	9.11E-13	15.38	42164	0	0	3300.8	1	1.69	0.1	23.934	2.6376	1.91131E-08	
27	41	4000	0.75	1400	30	4.82E-10	35.87	42164	1.00E-05	0	3301.2	1	0.73	0.1	23.934	2.6363	8.19135E-09	
28	73	4000	1	1400	30	3.23E-15	26.9	42164	0	0	3301	1	0.97	0.1	23.934	2.6368	1.09218E-08	
29	113	4000	1.25	1600	30	3.06E-13	24.88	42164	0	0	3381.2	1	1.21	0.1	23.934	2.6369	1.19457E-08	
30	145	4000	1.5	1600	30	1.46E-14	20.74	42164	0	0	3381.1	1	1.45	0.1	23.934	2.6373	1.43349E-08	
31	17	4000	0.5	1800	30	3.95E-08	62.04	42163	3.00E-05	0	3382	1	0.49	0.1	23.933	2.6332	4.77829E-09	
32	177	4000	1.75	1800	30	2.61E-13	17.78	42164	0	0	3381.1	1	1.69	0.1	23.934	2.6373	1.6724E-08	
33	49	4000	0.75	1600	30	2.36E-09	41.42	42164	1.00E-05	0	3381	1	0.73	0.1	23.935	2.638	7.16743E-09	
34	81	4000	1	1600	30	1.30E-08	31.1	42163	2.00E-05	0	3381.3	1	0.97	0.1	23.934	2.6364	9.55657E-09	
35	121	4000	1.25	1800	30	7.07E-10	28.24	42164	0	0	3445	1	1.21	0.1	23.934	2.6367	1.06184E-08	
36	153	4000	1.5	1800	30	2.77E-09	23.54	42164	2.00E-05	0.001	3444.9	1	1.45	0.1	23.934	2.637	1.27421E-08	
37	185	4000	1.75	1800	30	2.61E-12	20.18	42164	0	0	3444.9	1	1.69	0.1	23.934	2.6373	1.48658E-08	
38	57	4000	0.75	1800	30	2.21E-12	47.02	42164	0	0	3445.3	1	0.73	0.1	23.934	2.6352	6.37108E-09	

Graphs for Equations

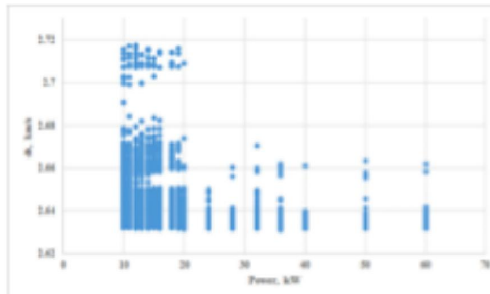


Figure 1. Power versus ΔV for GTO to GEO with shadowing on.

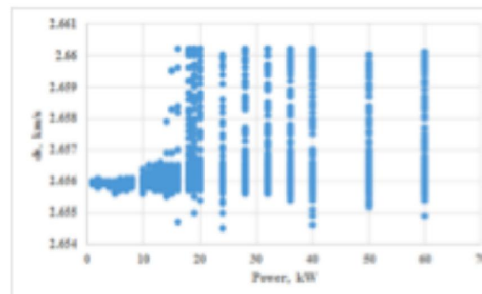


Figure 2. Power versus ΔV for GTO to GEO with shadowing off.

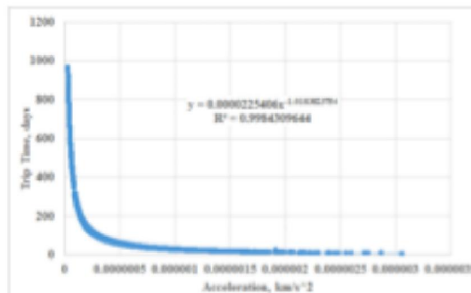


Figure 3. Trip time in terms of acceleration for GTO to GEO shadow on.

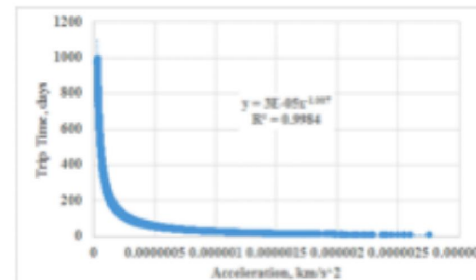


Figure 4. Trip time in terms of acceleration for GTO to GEO shadow off.

GTO to GEO Equations

Delta V

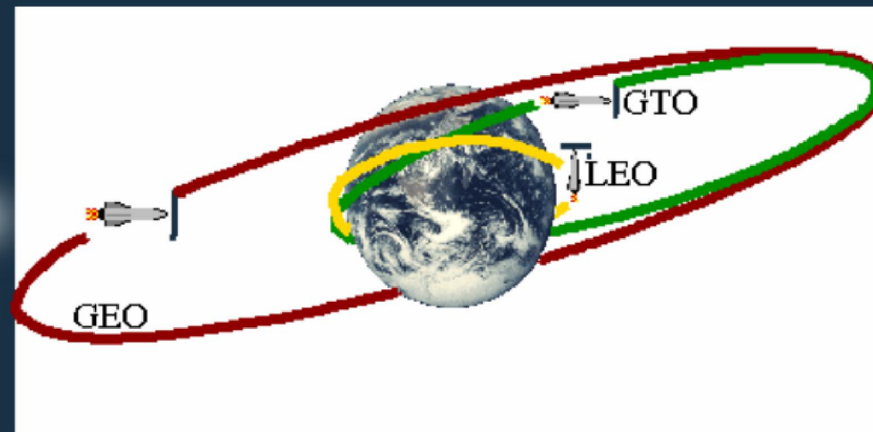
$$\Delta V = 2.65$$

Trip Time

as a function of start mass, power, efficiency, and
specific impulse:

$$t = (2 \times 10^{-5}) \left(\frac{2\eta p}{m_0 g I_{sp}} \right)^{-1.018}$$

Incremented Apogee



$$c = -0.44 \ln(a) + 5.6203$$

$$t = (c)(2 \times 10^{-5}) \left(\frac{2\eta p}{m_o g l_{sp}} \right)^{-1.018}$$

*When does low-thrust
propulsion make more sense
than chemical?*

We have to look at mass utilization and
the time-value of the mission to find
the optimal solution.

Sensitivity Analyses

- Power
- Start mass
- Specific impulse
- Efficiency
- Cost
- Revenue (\$k/kg) of payload
- Launch costs (for specific vehicles)

Spacecraft Model

Propulsion Wet Mass, kg	979.7339566. This was found by adding the tank mass, the propellant mass, and the total propulsion dry mass.
SEP Radiator Mass, kg	17.76669319. This was found by subtracting the PPU efficiency from 1 and multiplying it by the maximum SEP power and 1000, dividing it by 5.67×10^{-8} , multiplying it by radiator emissivity, dividing it by the difference of the radiator temperature to the fourth and the environment temperature to the fourth, dividing it by two, and multiplying it by the radiator areal density.
Battery Mass, kg ¹¹	0.001333333
Power BOP Mass, kg	40. This is an estimate.
Avionics Mass, kg	50. This is an estimate.
Dry Mass w/o Structure and Tanks, kg	912.7709984. This is the sum of the total propulsion dry mass without tank, the array mount and tilt mass, the SEP radiator mass, the battery mass, the power BOP mass, the avionics mass, and the solar array mass.
Structure Mass, kg	139.4382183. This is calculated by multiplying the structures percentage by the sum of the dry mass without structure and tanks and the tank mass.
Delta V, km/s	2.65. This is derived from the SEPSPT curves.
Ideal Final mass, kg	3655.5632362. This was found by taking the exponential of the product of 1000 and the ΔV and the reciprocal of the gravitational constant multiplied the specific impulse and multiplying it by the initial mass.
Starting specific power, W/kg	0.01. This was found by dividing the maximum SEP power by the start mass.
Starting acceleration, m/s ²	4.41726E-07. This was found with the Rocket Equation. The calculation was 2 times the efficiency and power of the spacecraft divided by g, the initial mass, and the specific impulse.
Total Propellant Mass, kg	373.713861. This is the propellant residual mass added to the difference of the start mass and final mass.
Propellant Residual Mass, kg	29.27712275. This is the difference of the start and final spacecraft mass multiplied by the propellant and residuals percentages.
Required Propellant, kg	344.4367383. This is calculated by subtracting the final mass from the initial mass.
Tank Mass, kg	16.81712375. This is calculated by multiplying the total propellant by the tank mass fraction.
Trip Time, Days	66.77740889. This is derived from the SEPSPT curves.
Total SEP Wet Mass, kg	1442.740201. This is the sum of the dry mass without the structure and tanks, the structure mass, the tank mass, and the propellant mass.
Non-SEP Mass, kg	2557.259799. This is the total SEP wet mass subtracted from the initial mass.
Partial SEP Cost, \$K	\$94,240.71. This is the sum of costs of the solar array, the product of the hardware per string and the

Launch Vehicles



Atlas V 551

\$190 million



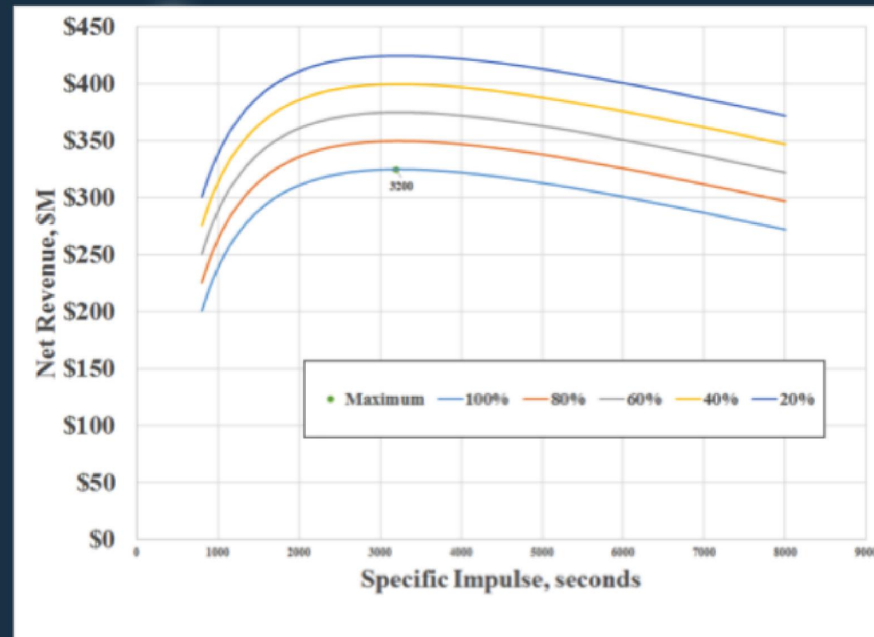
Falcon 9

\$61 million



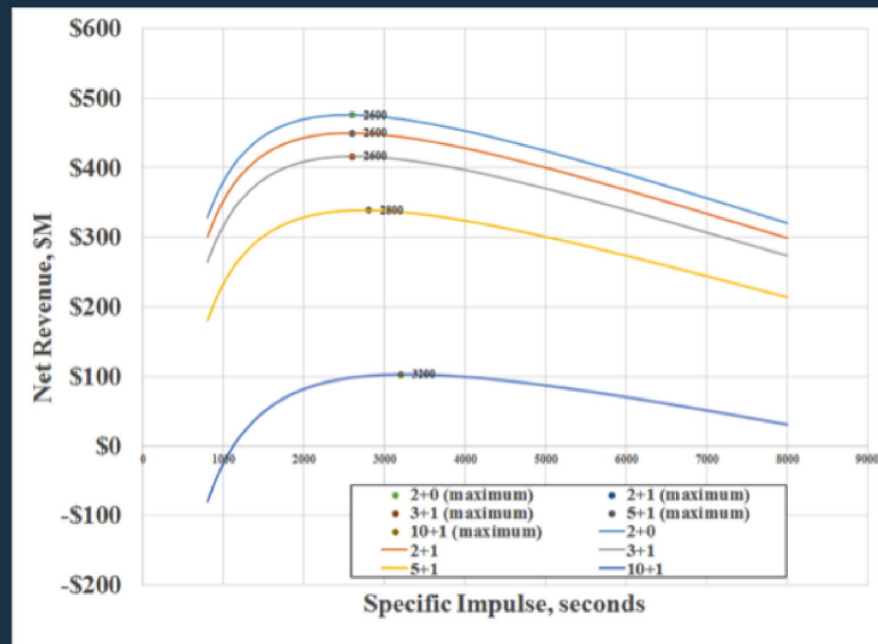
Prezi

Falcon 9



launch cost

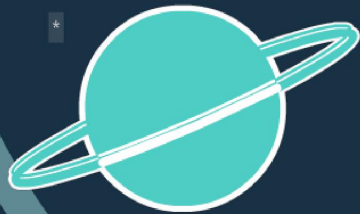
Atlas V 551



thruster quantity

Applicability

Will be used to guide future space architecture assessments.



Prezi

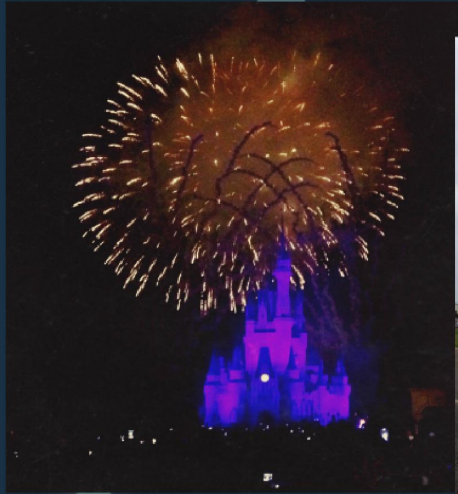


thank you!

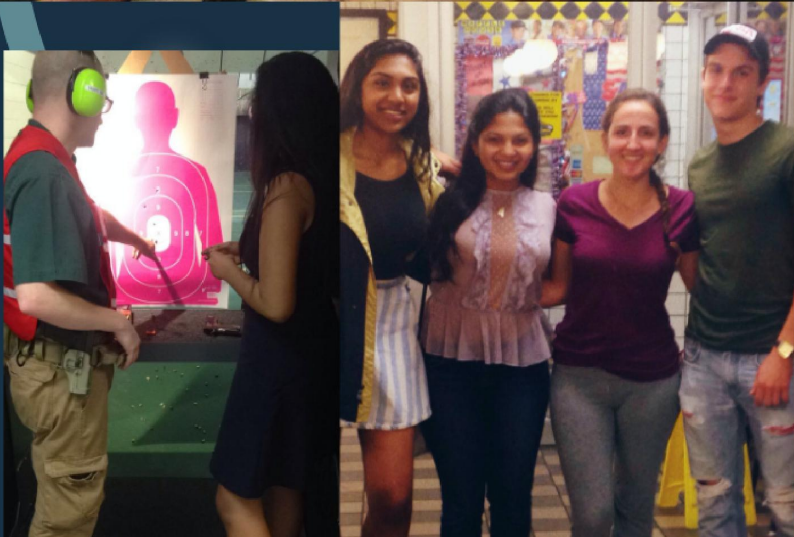
CineSpace and Hoot



Florida



Fun



There's ours 🤔🇺🇸🚀

Michoud and Johnson

